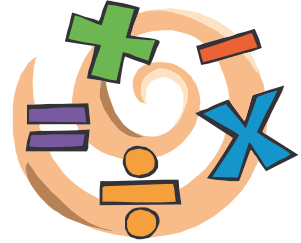


01

The number N is a multiple of 4. It lies between 10 and 40. 3 is a factor of N . When 4 is added to N , it becomes a multiple of 7.

- a) Find N
- b) Find the smallest number that should be subtracted from N to make it a multiple of 5



Your solution here:

02

A number P has exactly 3 factors. P is between 10 and 30. Find P .

Your solution here:



03 Mrs. Tina age now is a multiple of 4. She is younger than 50 years old and is twice as old as Mrs. Kavya now. Next year Mrs. Tina age will be a multiple of 5. How old was Mrs. Kavya last year ?



Your solution here:

04

- a) Have you noticed that $A \times B$ is a multiple of A and a multiple of B ?

Using numbers between 0 and 10 for A and B, give

- i) an example where $A \times B$ is not the smallest common multiple of A and B,
- ii) an example where $A \times B$ is not the smallest common multiple (but still a common multiple) of A and B.



In the second case, is there any relationship between the smallest common multiple of A and B and the actual value of $A \times B$?

- b) Using the above mentioned facts as clues, find a number which leaves a remainder of 9 when divided by 10, a remainder of 8 when divided by 9 and a remainder of 7 when divided by 8.

Your solution here:

05

★ □ ○ is a 3-digit number with digits ★ , □ , ○ .

★ is a multiple of 4 and ★ + □ + ○ = 21, ★ □ ○ is a multiple of 4 and 6.

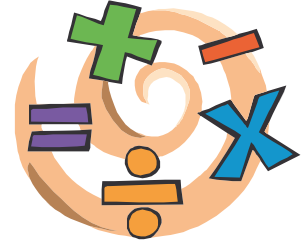
a) Is ★ □ ○ an odd or even number ?

b) Find the value of ★ □ ○

Your solution here:

01 The number N is a multiple of 4. It lies between 10 and 40. 3 is a factor of N . When 4 is added to N , it becomes a multiple of 7.

- a) Find N
- b) Find the smallest number that should be subtracted from N to make it a multiple of 5



- a) N is a multiple of 3 and 4

Multiples of 3 : 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 36, 39

Multiples of 4 : 4, 8, 12, 16, 20, 24, 28, 32, 36

$12 + 4 = 16$; $24 + 4 = 28$; $36 + 4 = 40$

Only 28 is a multiple of 7

Hence, $N = 24$

Shortcut : 12 is the 1st multiple of 3 and 4. The next common multiples will be 2×12 , 3×12 and so on.

- b) $N - 0 = 24$ (Not a multiple of 5)

$N - 1 = 23$ (Not a multiple of 5)

$N - 2 = 22$ (Not a multiple of 5)

$N - 3 = 21$ (Not a multiple of 5)

$N - 4 = 20$ (Multiple of 5, $20 \div 5 = 4$)

Therefore, the smallest number that should be subtracted is 4

Shortcut : Numbers that are multiples of 5 always have 0 or 5 as the last digit

02

A number P has exactly 3 factors. P is between 10 and 30. Find P.

[Tip : Usually factors will appear in pairs. If there are an odd number of factors, the original number should be of the form $A \times A$, So that atleast there are 3 factors that are 1, A and $(A \times A)$ itself]

$3 \times 3 = 9$ (ignore as it is not in the range);

$4 \times 4 = 16$; $5 \times 5 = 25$

Factors of 16 : 1, 2, 4, 8, 16 (5 factors)

Factors of 25 : 1, 5, 25 (3 factors)

Therefore, $P = 25$



03

Mrs. Tina age now is a multiple of 4. She is younger than 50 years old and is twice as old as Mrs. Kavya now. Next year Mrs. Tina age will be a multiple of 5. How old was Mrs. Kavya last year ?



Note that Mrs. Tina and Mrs Kavya indicate they are adults

Multiple of 4 indicates an even number

Since Mrs. Tina's age + 1 year is a multiple of 5 (which ends with a '5' or '0' only), Mrs. Tina's age now must end with '4'

Mrs. Tina is younger than 50 years old now and she is an adult, so the possible age is either 24 or 44

$$24 \div 2 = 12; 44 \div 2 = 22$$

Mrs. Kavya should be 22 years old now since she is also an adult

$$22 - 1 = 21. \text{ Mrs. Kavya was 21 years old last year}$$

04

- a) Have you noticed that $A \times B$ is a multiple of A and a multiple of B ?

Using numbers between 0 and 10 for A and B, give

- i) an example where $A \times B$ is not the smallest common multiple of A and B,
- ii) an example where $A \times B$ is not the smallest common multiple (but still a common multiple) of A and B.



In the second case, is there any relationship between the smallest common multiple of A and B and the actual value of $A \times B$?

- b) Using the above mentioned facts as clues, find a number which leaves a remainder of 9 when divided by 10, a remainder of 8 when divided by 9 and a remainder of 7 when divided by 8.

- a) i) $A = 3, B = 4: A \times B = 12$. 12 is the smallest common multiple of 3 and 4. (This happens when A and B have no common factor other than 1)

- ii) $A = 4, B = 6: A \times B = 24$, which is a common multiple of 4 and 6

24 is a multiple of 12, which is the smallest common multiple of 4 and 6

- b) Note that the answer should be 1 less than a common multiple of 10, 9 and 8

A common multiple of 8 & 9 : $8 \times 9 = 72$

A common multiple of 8, 9 & 10 is $72 \times 10 = 720$

(The smallest common multiple of 8, 9 & 10 is 360)

One answer is : $720 - 1 = 719$

05

★ □ ○ is a 3-digit number with digits ★ , □ , ○ .
★ is a multiple of 4 and ★ + □ + ○ = 21, ★ □ ○ is a multiple of 4 and 6.

- a) Is ★ □ ○ an odd or even number ?
b) Find the value of ★ □ ○

- a) ★ □ ○ is an even number as it is a multiple of 4
b) ★ has to be 4 or 8 only since it is a multiple of 4

Since ★ + □ + ○ = 21

if ★ = 4, □ + ○ = 17 and

if ★ = 8, □ + ○ = 13

You will see that only 498, 876 and 894 satisfy the above two conditions and the fact that the number is even.

Of these numbers, only 876 is a multiple of both 4 and 6

So, ★ □ ○ = 876